# Mathematics <br> November 2022 Practice Paper 1 (Non-Calculator) 

Higher Tier

## Time: 1 hour 30 minutes

You must have: Ruler graduated in centimetres and millimetres, protractor, pair of compasses, pen, HB pencil, eraser.

## Instructions

- Use black ink or ball-point pen.
- Fill in the boxes at the top of this page with your name, centre number and candidate number.
- Answer all questions.
- Answer the questions in the spaces provided
- there may be more space than you need.
- Calculators may not be used.

- Diagrams are NOT accurately drawn, unless otherwise indicated.
- You must show all your working out.


## Information

- The total mark for this paper is 80
- The marks for each question are shown in brackets
- use this as a guide as to how much time to spend on each question.


## Advice

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end.


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## Higher Tier Formulae Sheet

## Perimeter, area and volume

Where $a$ and $b$ are the lengths of the parallel sides and $h$ is their perpendicular separation:

$$
\text { Area of a trapezium }=\frac{1}{2}(a+b) h
$$

Volume of a prism $=$ area of cross section $\times$ length Where $r$ is the radius and $d$ is the diameter:

Circumference of a circle $=2 \pi \mathrm{r}=\pi d$
Area of a circle $=\pi r^{2}$

## Pythagoras' Theorem and Trigonometry


b


## Quadratic formula

The solution of $a x^{2}+b x+c=0$
where $a \neq 0$

$$
x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}
$$

In any right-angled triangle where $a, \mathrm{~b}$ and $c$ are the length of the sides and c is the hypotenuse:

$$
a^{2}+b^{2}=c^{2}
$$

In any right-angled triangle $A B C$ where $a, b$ and $c$ are the length of the sides and $c$ is the hypotenuse:

$$
\sin A=\frac{a}{c} \quad \cos A=\frac{b}{c} \quad \tan A=\frac{a}{b}
$$

In any triangle ABC where $\mathrm{a}, \mathrm{b}$ and c are the length of the sides:
sine rule: $\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$
cosine rule: $a^{2}=b^{2}+c^{2}-2 b c \cos A$
Area of triangle $=\frac{1}{2} a b \sin C$

## Probability

Where $\mathrm{P}(A)$ is the probability of outcome $A$ and $\mathrm{P}(B)$ is the probability of outcome $B$ :

$$
\begin{aligned}
& \mathrm{P}(A \text { or } B)=\mathrm{P}(A)+\mathrm{P}(B)-\mathrm{P}(A \text { and } B) \\
& \mathrm{P}(A \text { and } B)=\mathrm{P}(A \text { given } B) \mathrm{P}(B)
\end{aligned}
$$

1 Work out $37.1 \times 9.3$

$$
\begin{array}{r}
371 \\
\times \quad 93 \\
\hline 1413 \\
33390 \\
\hline 34503
\end{array}
$$

2 Write 72 as a product of its prime factors.


3 Sam is ordering pizza for all the people in her company.
Sam takes a sample of 50 people in the company.
She asks them which pizza they would like to order.
The table shows information about the results.

| Pizza | Number of People |
| :---: | :---: |
| Margarita | 19 |
| Vegetable | 13 |
| Pineapple | $\underline{8}$ |
| Pepperoni | 10 |

There are 600 people in the company
(a) Work out how many Pineapple pizzas Sam should order

(b) Write down any assumption you made and explain how this could affect your answer.

1 assumed the 50 people in the sample are representitive of all The people in the company If they are not the answer would not be accurate.

4 In a bag there are blue sweets, red sweets and green sweets.
The ratio of blue sweets to red sweets to green sweets is 5:3:2
What fraction of the sweets are green?

5 (a) Work out $5 \times \frac{3}{4}-\frac{7}{10} \times 2$

$$
\frac{15}{20}-\frac{14}{20}
$$

$\frac{1}{20}$
(2)
(b) Work out $2 \frac{1}{3} \times \frac{3}{5}$

Give your answer as a mixed number in its simplest form.

$$
\frac{7}{3_{1}} \times \frac{8^{1}}{5}=\frac{7}{5}=1 \frac{2}{5}
$$



6 A block exerts a force of 84 Newtons on a table.
The pressure on the table is $112 \mathrm{~N} / \mathrm{m}^{2}$.
Work out the area of the box that is in contact with the table.

$$
\text { pressure }=\frac{\text { force }}{\text { area }}
$$

$$
\begin{aligned}
\text { area } & =\frac{\text { force }}{\text { pressure }} \\
& =\frac{84}{112}=\frac{42}{56}=\frac{21}{28}=\frac{3}{4}
\end{aligned}
$$

$\square$

.................. 0.75
(Total for Question 6 is 2 marks)
$7 \begin{aligned} & \text { Andy and Bruce share some sweets in the ratio 9:4. } 13 \text { parts } \\ & \text { Andy gets } A \text { sweets }\end{aligned}$ $\times 7$

Bruce gets $B$ sweets
Carla and David share the same amount of sweets as Andy and Bruce.
They share their sweets in the ratio 5:2.
Carla gets $C$ sweets
David gets $D$ sweets
Find $A: B: C: D$

$$
\begin{aligned}
& C: D \\
& \text { 5:2 } \\
& \text { 65:26 } \\
& \text { 63:28 } \\
& A: B: C: D \\
& \text { 63:28:65:26 }
\end{aligned}
$$

$$
63: 28: 65: 26
$$

(Total for Question 7 is 3 marks)

(a) Rotate trapezium $\mathbf{T} 180^{\circ}$ about the origin.

Label the new trapezium $\mathbf{A}$.
(b) Translate trapezium $\mathbf{T}$ by the vector $\binom{-1}{-3}$
Label the new trapezium $\mathbf{B}$.

9
$\mathbf{A}=2^{2} \times 3 \times 5^{2} \quad \mathbf{B}=2^{3} \times 3^{2} \times 7$
(a) Write down the highest common factor (HCF) of $\mathbf{A}$ and $\mathbf{B}$.

$$
2^{2}+3
$$

$\qquad$
(b) Find the lowest common multiple (LCM) of $\mathbf{A}$ and $\mathbf{B}$.

$$
\begin{gathered}
2^{3} \times 3^{2} \times 5^{2} \times 7 \\
8 \times 9 \times 25 \times 7 \\
72 \times 175
\end{gathered}
$$


(Total for Question 9 is $\mathbf{3}$ marks)
$10 \quad s=u t+\frac{1}{2} a t^{2}$
$u=-5$
$a=4$
$t=3$
Work out the value of $s$.

$$
\begin{aligned}
S & =(-5)(3)+\frac{1}{2}(4)(3)^{2} \\
& =-15+2(9) \\
& =-15+18 \\
& =3
\end{aligned}
$$

$$
s=3
$$

(Total for Question 10 is 2 marks)

11 Sweets are sold in small packs and in big packs.
There is a total of 175 sweets in 4 small packs and 3 big packs.
There is a total of 154 sweets in 5 small packs and 2 big packs.
Work out the number of sweets in each small pack and in each big pack.

$$
\begin{array}{rlrl}
4 s+3 b & =175 & \times 2 \\
5 s+2 b & =154 & \times 3 \\
5 s+6 b & =350 & \\
15 s+6 b & =462 & 5(16)+2 b=154 \\
7 s & =112 & 80+2 b=154 \\
s & =\frac{112}{7} & 2 b & =74 \\
15 & &
\end{array}
$$

$$
7 \frac{016}{1,2}
$$

Small Pack ...............6...................

$$
s=16
$$

Big Pack $\qquad$
(Total for Question 11 is $\mathbf{3}$ marks)

12 Given that $3 \times \sqrt{27}=3^{n}$
Find the value $n$.

$$
\begin{aligned}
& \sqrt{27}=\sqrt{3^{3}}=3^{\frac{3}{2}} \\
& 3^{1} \times 3^{\frac{3}{2}}=3^{\frac{5}{2}}
\end{aligned}
$$

$$
\frac{5}{2}
$$

(Total for Question 12 is 2 marks)

13 (a) Complete the table of values for $y=x^{3}+3 x$

| $x$ | -2 | -1 | 0 | 1 | 2 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | -14 | -4 | 0 | 4 | 14 |

(b) On the grid, draw the graph of $y=x^{3}+3 x$


14 In a bag there are only red counters, blue counters, green counters and yellow counters.
A counter is taken at random from the bag.
The table shows the probabilities that the counter will be green or will be yellow.

| Colour | Red | Blue | Green | Yellow |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Probability | $2 \boldsymbol{x}$ | $x$ | 0.35 | 0.20 |  |  |
|  |  |  |  |  |  |  |

The probability that the counter will be red is twice the probability that the counter will be blue.
There are 21 green counters in the bag.
Work out the number of red counters in the bag.

$$
\begin{aligned}
2 x+x+0.35+0.2 & =1 \\
3 x+0.55 & =1 \\
3 x & =0.45 \\
x & =0.15 \\
2 x & =0.3
\end{aligned}
$$

$\begin{aligned} \div 35 \% \text { of counters } & =21 \\ 5 \% \text { or counter } & =3\end{aligned}$

$$
21-3=18
$$

$30 \%$ of counters $=18$

15 The diagram shows a rectangle.
$2 x+3$


All the measurements are in centimetres.
The area of the rectangle is $75 \mathrm{~cm}^{2}$
Work out the value of $x$.
You must show all your working.

$$
\begin{array}{r}
(2 x+3)(3 x-3)=75 \\
6 x^{2}-6 x+9 x-9=75 \\
6 x^{2}+3 x-9=75 \\
6 x^{2}+3 x-84=0 \\
2 x^{2}+x-28=0 \\
(2 x-7)(x+4)=0 \\
x=\frac{7}{2} x=-4 \\
x \\
\text { cannot have } \\
\text { negative length }
\end{array}
$$

16 A population of bacteria is increasing by $10 \%$ each hour.
Find the percentage increase in the population every 3 hours.

$$
\begin{array}{lll}
\frac{100}{10}=10 & 110 & 1 \text { hour } \\
\frac{110}{10}=11 & 121 & 2 \text { hours } \\
\frac{121}{10}=12.1 & 133.1 & 3 \text { hours } \\
& &
\end{array}
$$

17 Show that $(3-\sqrt{8})(5+\sqrt{18})$ can be written in the form $a+b \sqrt{2}$

$$
\begin{aligned}
& \sqrt{8}=\sqrt{4} \sqrt{2}=2 \sqrt{2} \\
& \sqrt{18}=\sqrt{9} \sqrt{2}=3 \sqrt{2} \\
& (3-2 \sqrt{2})(5+3 \sqrt{2}) \\
& 15+9 \sqrt{2}-10 \sqrt{2}-12 \\
& 3-\sqrt{2}
\end{aligned}
$$

(Total for Question 17 is 3 marks)

18 Sketch the graph of $y=\sin x^{\circ}$ for $0 \leq x \leq 360$


19 Solve $\frac{8}{3 x-2}+\frac{6}{x+1}=2$

$$
\begin{aligned}
8(x+1)+6(3 x-2) & =2(3 x-2)(x+1) \\
8 x+8+18 x-12 & =2\left(3 x^{2}+3 x-2 x-2\right) \\
26 x-4 & =2\left(3 x^{2}+x-2\right) \\
13 x-2 & =3 x^{2}+x-2 \\
0 & =3 x^{2}-12 x \\
0 & =3 x(x-4) \\
x & =0 \quad x=4
\end{aligned}
$$

$$
x=0 \text { or } x=4
$$

20 AOB is a sector of a circle, centre $O$ and radius 18 cm . The angle of the sector is $125^{\circ}$.


Calculate the length of the arc $A B$.
Give your answer in terms of $\pi$.

$$
\begin{aligned}
& \frac{125}{360} \times 2 \pi(18) \\
& \frac{125}{360} \times 36 \pi \\
& \frac{125}{10} \times \pi \\
& 12.5 \pi
\end{aligned}
$$

$12.5 \pi$

$$
\mathrm{cm}
$$

(Total for Question 20 is 2 marks)
$21 x$ is inversely proportional to the square root of $y$
When $x=12, y=9$
Find the value of $x$ when $y=81$

$$
\begin{aligned}
x & =\frac{k}{\sqrt{y}} & x & =\frac{36}{\sqrt{y}} \\
12 & =\frac{k}{\sqrt{9}} & x & =\frac{36}{\sqrt{81}} \\
12 & =\frac{k}{3} & & =\frac{36}{9} \\
k & =36 & & =4
\end{aligned}
$$

$$
x=\ldots
$$


$A$ and $C$ are points on the circumference of a circle, centre $O$.
$B C$ is a tangent to the circle.
Angle $C A B=29^{\circ}$
Find the size of angle $A B C$.
You must show all your working.
$O C B=90^{\circ}$ Tangent meets radius ot $90^{\circ}$
$A C O=29^{\circ}$ Angles at the base of an isosceles triangle are equal
$2 \times 29=58^{\circ} \quad$ Angles in a triangle add to $180^{\circ}$
180-58 $=122^{\circ}$ Angles on a straight line add to $180^{\circ}$
$180-90-58=32^{\circ} \quad \begin{aligned} & \text { Angles in a triangle } \\ & \text { add to } 180^{\circ}\end{aligned}$

23 The diagram shows a solid shape.
The shape is a cone on top of a hemisphere.


The height of the cone is 12 cm .
The base of the cone has a diameter of $10 \mathrm{~cm} . r=5$
The diameter of the hemisphere is 10 cm .
Work out the total volume of the solid shape.
Give your answer in terms of $\pi$.
Hemisphere
Cone

$$
\begin{aligned}
V & =\frac{2}{3} \pi r^{3} \\
& =\frac{2}{3} \pi(5)^{3} \\
& =\frac{2}{3} \pi(125) \\
& =\frac{250}{3} \pi
\end{aligned}
$$

$$
v=\frac{1}{3} \pi r^{2} h
$$

$$
=\frac{1}{3} \pi(5)^{2}(12)
$$

$$
\begin{aligned}
& =4 \pi(25) \\
& =100 \pi
\end{aligned}
$$

$$
\begin{aligned}
\text { Total } V & =\frac{250}{3} \pi+100 \pi \\
& =\left(\frac{250}{3}+\frac{300}{3}\right) \pi \\
& =\frac{550}{3} \pi
\end{aligned}
$$

24 The histogram shows information about the weight of pigs.


30 pigs weigh between 50 and 65 kg .
(a) Work out an estimate for the number of pigs which weigh more than 80 kg .

$$
\begin{array}{ll}
\frac{30}{15}=2 & 5 \times 4=20 \\
15 \times 1 & =15
\end{array} \quad 20+15=35
$$

$$
\begin{equation*}
35 \tag{3}
\end{equation*}
$$

(b) Explain why your answer to part a is only an estimate.
(3)
 80 and 85 kg ......We estimated it is half the $7.5 \mathrm{~K} . \mathrm{k} .1 \mathrm{~m} .8 \mathrm{~kg}$ group.

25 Here are seven number cards.


Helen takes a card at random.
She does not replace the card.
Helen then takes another card at random.
Calculate the probability that the number on the second card Helen takes is greater than the number on the first card she takes.

$$
\begin{aligned}
P(1,2)= & \frac{2}{7} \times \frac{2}{6}=\frac{4}{42} \\
P(1,3)= & \frac{2}{7} \times \frac{3}{6}=\frac{6}{42} \\
P(2,3)= & \frac{2}{7} \times \frac{3}{6}=\frac{6}{42} \\
& \frac{4}{42}+\frac{6}{42}+\frac{6}{42}=\frac{16}{42}
\end{aligned}
$$

26


Work out the value of $x$.
Give your answer as a simplified surd.

$$
\begin{aligned}
& \sin (60)=\frac{\sqrt{3}}{2} \\
& \sin (45)=\frac{\sqrt{2}}{2}
\end{aligned}
$$

$$
\begin{aligned}
\frac{x}{\sin (60)} & =\frac{8}{\sin (45)} \\
\frac{x}{\sqrt{3} / 2} & =\frac{8}{\sqrt{2} / 2} \\
x\left(\frac{\sqrt{2}}{2}\right) & =8\left(\frac{\sqrt{3}}{2}\right) \\
x \sqrt{2} & =\frac{8 \sqrt{3}}{\sqrt{2}} \\
x & =\frac{8 \sqrt{6}}{2} \\
& =\frac{4 \sqrt{6}}{x}
\end{aligned}
$$

