Surname

Other Names

Mathematics June 2023 Practice Paper 3 (Calculator) Higher Tier

Time: 1 hour 30 minutes

You must have: Ruler graduated in centimetres and millimetres, protractor, pair of compasses, pen, HB pencil, eraser, calculator. Tracing paper may be used.

Total Marks

Instructions

- Use **black** ink or ball-point pen.
- Fill in the boxes at the top of this page with your name,

centre number and candidate number.

- Answer **all** questions.
- Answer the questions in the spaces provided
- there may be more space than you need.
- Calculators may be used.
- Diagrams are **NOT** accurately drawn, unless otherwise indicated.
- You must show all your working.

Information

- The total mark for this paper is 80
- The marks for each question are shown in brackets
- use this as a guide as to how much time to spend on each question.

Advice

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end.



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Higher Tier Formulae Sheet

Perimeter, area and volume

Where a and b are the lengths of the parallel sides and h is their perpendicular separation:

Area of a trapezium = $\frac{1}{2}(a+b)h$

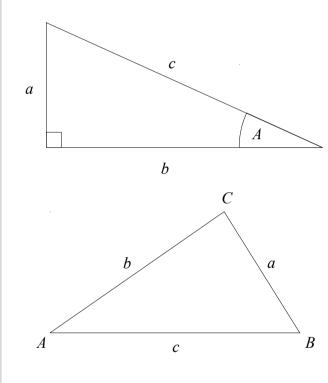
Volume of a prism = area of cross section \times length

Where r is the radius and d is the diameter:

Circumference of a circle = $2\pi r = \pi d$

Area of a circle = πr^2

Pythagoras' Theorem and Trigonometry



Compound Interest

Where P is the principal amount, r is the interest rate over a given period and n is number of times that the interest is compounded:

Total accrued =
$$P\left(1 + \frac{r}{100}\right)^{r}$$

END OF EXAM AID

Quadratic formula

The solution of $ax^2 + bx + c = 0$

where $a \neq 0$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

In any right-angled triangle where a, b and c are the length of the sides and c is the hypotenuse:

 $a^2 + b^2 = c^2$

In any right-angled triangle ABC where a, b and c are the length of the sides and c is the hypotenuse:

$$\sin A = \frac{a}{c} \quad \cos A = \frac{b}{c} \quad \tan A = \frac{a}{b}$$

In any triangle ABC where a, b and c are the length of the sides:

sine rule:
$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

cosine rule:
$$a^2 = b^2 + c^2 - 2bc \cos A$$

Area of triangle = $\frac{1}{2}ab\sin C$

Probability

Where P(A) is the probability of outcome A and P(B) is the probability of outcome B:

P(A or B) = P(A) + P(B) - P(A and B)

$$P(A \text{ and } B) = P(A \text{ given } B) P(B)$$

(
1	$A = 2^3 \times 3^2 \times 5$	$B = 2^2 \times 3^3 \times 5$		
	Write down the highes	t common factor (HCF) of A	A and B	
			(Total for Question 1 is 1 m	arlı)
				атк)
2	Verity buys 12 bottles Verity sells all 12 bottl	of apple juice for a total cos es at £1.75 each bottle.	t of £15	
	Work out Verity's perc	entage profit.		
			(Total for Question 2 is 3 m	narks)

The table shows the populations of five countries.

Country	Population
India	1.4×10^{9}
Turkey	8.4×10^{7}
Denmark	$5.8 imes10^6$
Estonia	$1.3 imes 10^6$
Iceland	3.4×10^{5}

(a) Work out the difference between the population of India and the population of Turkey. Give your answer in standard form.

(2)

Given that

3

population of Iceland = $\frac{1}{k}$ × population of Denmark

(b) Work out the value of *k*.

Give your answer correct to the nearest whole number.

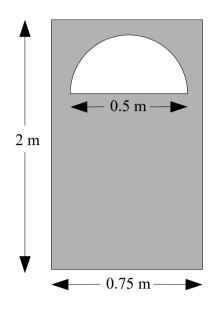
k =

(2)

(Total for Question 3 is 4 marks)

The diagram shows the front of a wooden door with a semicircular glass window.

4



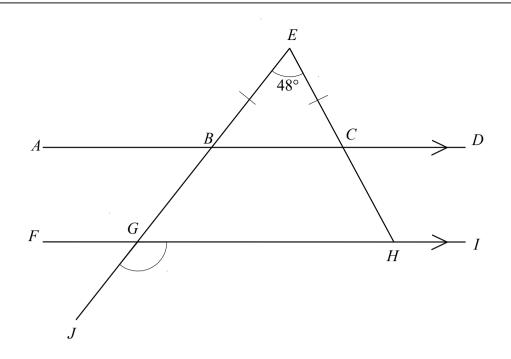
Julie wants to apply 2 coats of wood varnish to the front of the door, shown shaded in the diagram.

250 millilitres of wood varnish covers 4 m^2 of the wood.

Work out how many millilitres of wood varnish Julie will need. Give your answer correct to the nearest millilitre.

millilitres

(Total for Question 4 is 5 marks)



ABCD and *FGHI* are parallel straight lines. *EBGJ* and *ECH* are straight lines.

BE = CEAngle $BEC = 48^{\circ}$

Work out the size of angle *JGH*. Give a reason for each stage of your working.

(Total for Question 5 is 5 marks)

0

5

	Adam drove 56 km from Liverpool to Manchester. He then drove 61 km from Manchester to Sheffield.						
	Adam's average speed from Liverpool to Manchester was 80 km/h. Adam took 85 minutes to drive from Manchester to Sheffield.						
	(a) Work out Adam's average speed for his total drive from Liverpool to Sheffield.						
			km/ł				
	Bev drove from Reading to Bristol.	(4)					
	Bev's average speed from Reading to Swindon was 80 km/h. Her average speed from Swindon to Bristol was 60 km/h.						
	Bev says that the average speed from Reading to Bristol can be found by working out the mean of 80 km/h and 60 km/h.						
	(b) If Bev is correct, what does this tell you about the two parts of Bev's journey?						
		(1)					
	(Total for Question 6 is 5 n	(asles)					

7 A company has to make a large number of boxes.

The company has 6 machines. All the machines work at the same rate. When all the machines are working, they can make all the boxes in 9 days.

2 of the machines are not working and cannot be used to make the boxes.

Work out the total number of days taken to make all the boxes.

(Total for Question 7 is 3 marks)

Janet bought a new car three years ago.

8

At the end of the first year the value of the car had decreased by 17.5% The value of the car decreased by 10% each year for the next two years.

At the end of the three years, the car was worth $\pounds 16038$

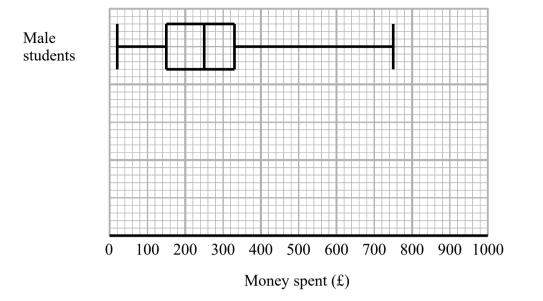
Work out the value of the car when Janet bought it three years ago.

(Total for Question 8 is 3 marks)

£

Simplify fully	$\left(\frac{16 x^4}{9 y^{10}}\right)^{-\frac{1}{2}}$					
				(Total for Q	uestion 9 is	3 marks)
Expand and sir	nplify $(2-x)($	(2x+3)(x+4)	·)			
Expand and sir	nplify (2 – <i>x</i>)((2x+3)(x+4)	·)			
Expand and sir	nplify (2 – <i>x</i>)((2x+3)(x+4)	•)			
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Expand and sin	nplify (2 – <i>x</i>)((2x+3)(x+4)	+) 			
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Expand and sin	nplify (2 – <i>x</i>)((2x+3)(x+4)	+) 		uestion 10 is	s 3 marks)

11 The box plot shows information about the distribution of the amounts of money spent by some male students on their holidays.



(a) Work out the interquartile range for the amounts of money spent by these male students.

(2)

£

The table below shows information about the distribution of the amounts of money spent by some female students on their holidays.

	Smallest	Lower quartile	Median	Upper quartile	Highest
Money spent (£)	60	180	300	350	650

(b) On the grid above, draw a box plot for the information in the table

(2)

Chris says,

"The box plots show that the female students spent more money than the male students."

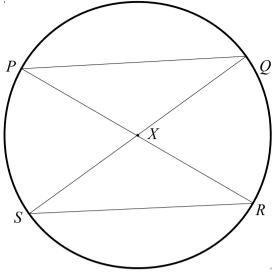
(c) Is Chris correct? Give a reason for your answer.

(Total for Question 11 is 5 marks)

(1)

12 Using algebra, show that the recurring de	cimal $0.18\dot{0}\dot{3} = \frac{119}{660}$
	000
	(Total for Question 12 is 2 marks)
13 Saffron wants to work out an estimate for On Friday, Saffron catches 210 fish from	
She puts a tag on each of these fish and p On Saturday, Saffron catches 240 fish fro	uts them back into the lake. m the same lake.
She finds that 35 of the 240 fish are tagge Work out an estimate for the total number	
	(Total for Question 13 is 3 marks)

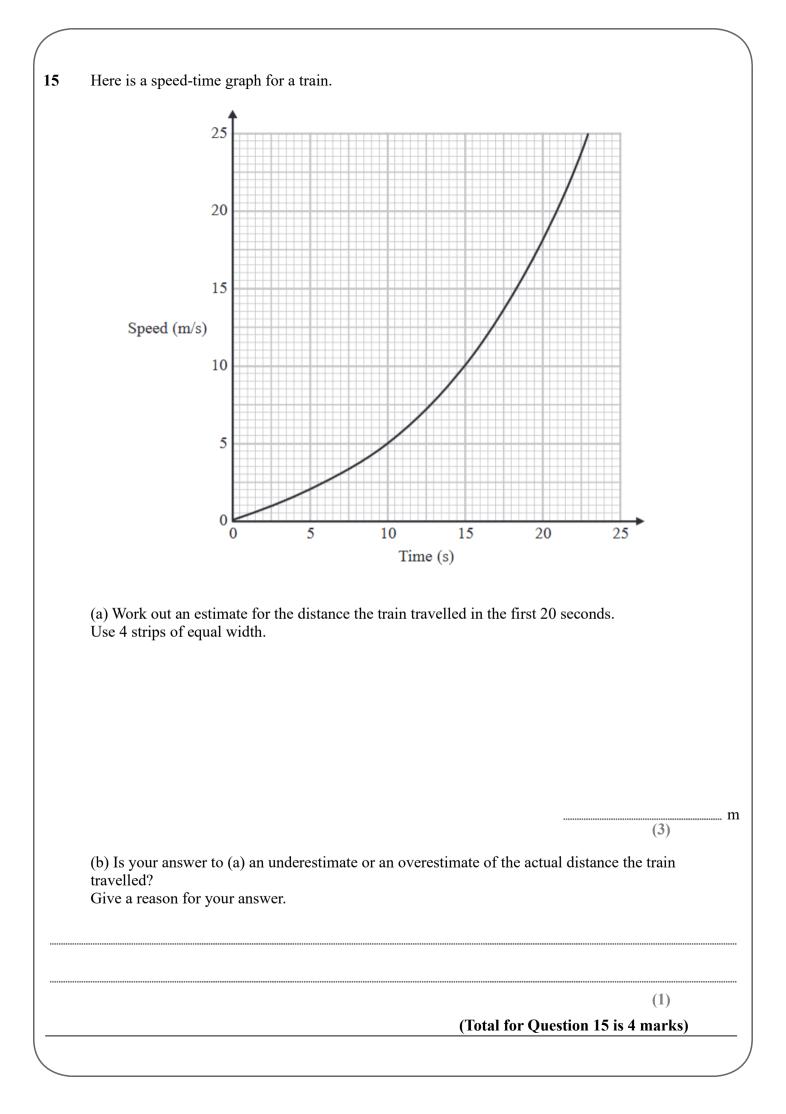
14 P, Q, R and S are four points on a circle, centre X.



PXR and *SXQ* are straight lines.

Prove that triangle *PQX* and triangle *SRX* are congruent.

(Total for Question 14 is 3 marks)



16 Using algebra, prove that, given any 3 consecutive even numbers, the difference between the square of the largest number and the square of the smallest number is always 8 times the middle number.

(Total for Question 16 is 3 marks)

17	The straight 1	ine L passes	through the p	points (4,	-2) and ((6, 5)
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The straight line M is perpendicular to L and intersects the y-axis at the point (0, 3)

Find the coordinates of the point where *M* intersects the *x*-axis.

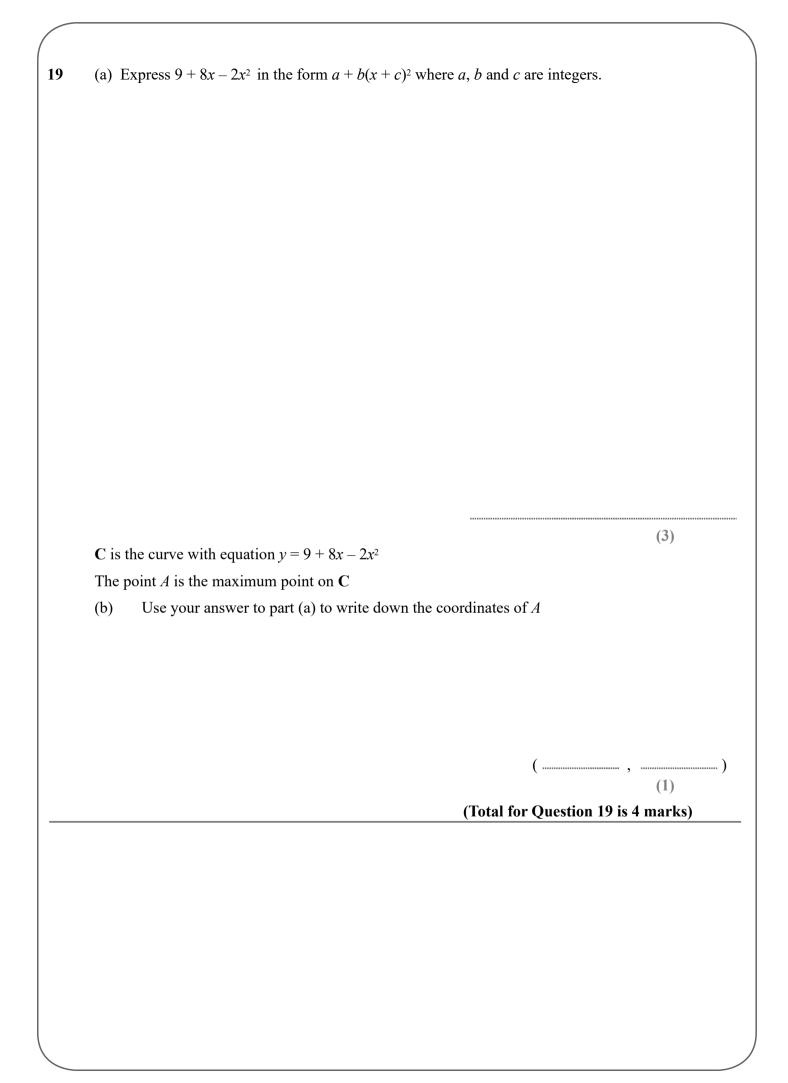
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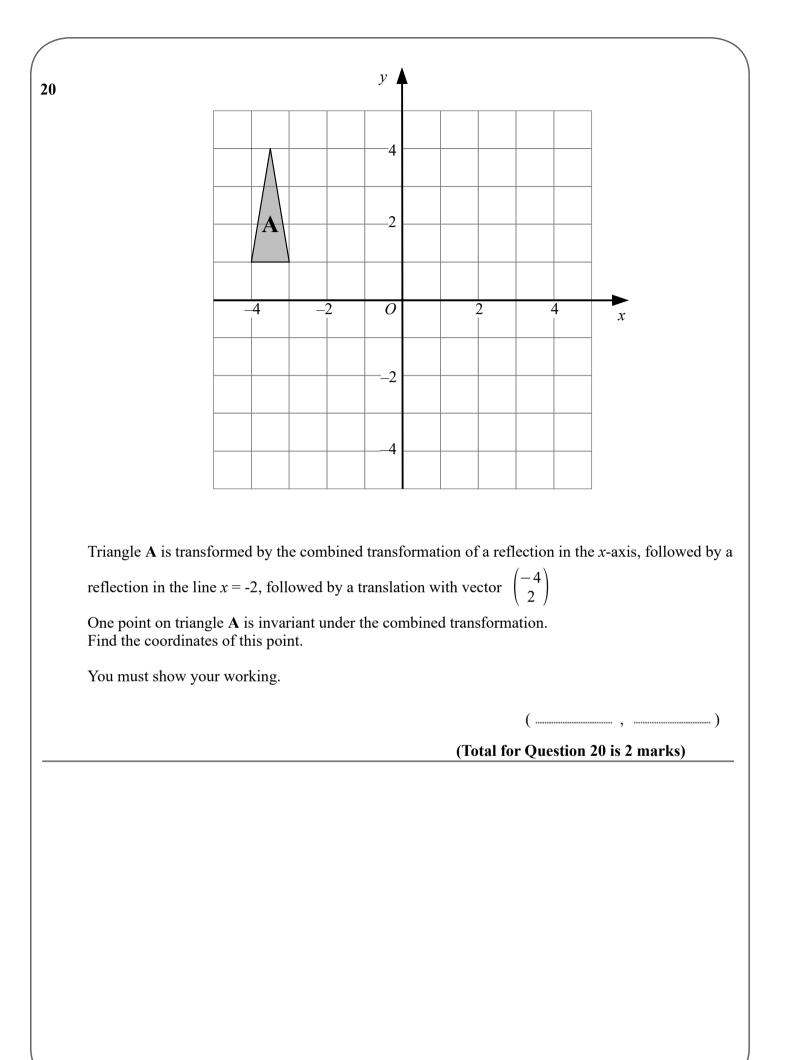
(Total for Question 17 is 4 marks)

18 Show that
$$\frac{x}{x+3} - \frac{2x-1}{x-3} + 1$$
 can be written in the form $\frac{ax+b}{x^2-9}$

where *a* and *b* are integers.

(Total for Question 18 is 4 marks)

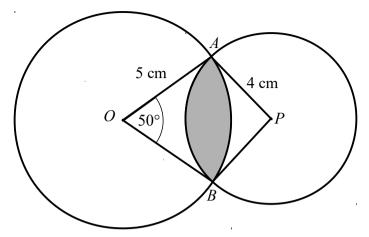




21 Prove algebraically that the straight line with equation 2x + y + 5 = 0 is a tangent to the circle with equation $x^2 + y^2 = 5$

(Total for Question 21 is 5 marks)

22 The diagram shows two circles such that the region **R**, shown shaded in the diagram, is the region common to both circles.



One of the circles has centre *O* and radius 5 cm. The other circle has centre *P* and radius 4 cm. Angle $AOB = 50^{\circ}$

Calculate the area of region **R**. Give your answer correct to 3 significant figures.

 $----cm^2$

(Total for Question 22 is 6 marks)

TOTAL FOR PAPER IS 80 MARKS