## Mathematics

## June 2024 Practice Paper 3 (Calculator) Foundation Tier

Time: 1 hour 30 minutes

You must have: Ruler graduated in centimetres and millimetres, protractor, pair of compasses, pen, HB pencil, eraser, calculator. Tracing paper may be used.

## Instructions

- Use black ink or ball-point pen.
- Fill in the boxes at the top of this page with your name, centre number and candidate number.
- Answer all questions.
- Answer the questions in the spaces provided
- there may be more space than you need.
- Calculators may be used.
- Diagrams are NOT accurately drawn, unless otherwise indicated.

- You must show all your working.


## Information

- The total mark for this paper is 80
- The marks for each question are shown in brackets
- use this as a guide as to how much time to spend on each question.


## Advice

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end.


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## Foundation Tier Formulae Sheet

## Perimeter, area and volume

Where $a$ and $b$ are the lengths of the parallel sides and h is their perpendicular separation:

$$
\text { Area of a trapezium }=\frac{1}{2}(a+b) h
$$

Volume of a prism $=$ area of cross section $\times$ length
Where $r$ is the radius and $d$ is the diameter:
Circumference of a circle $=2 \pi \mathrm{r}=\pi d$
Area of a circle $=\pi r^{2}$

## Pythagoras' Theorem and Trigonometry


b

In any right-angled triangle where $a, \mathrm{~b}$ and $c$ are the length of the sides and c is the hypotenuse:

$$
a^{2}+b^{2}=c^{2}
$$

In any right-angled triangle $A B C$ where $a, b$ and $c$ are the length of the sides and $c$ is the hypotenuse:

$$
\sin A=\frac{a}{c} \quad \cos A=\frac{b}{c} \quad \tan A=\frac{a}{b}
$$

## Probability

Where $\mathrm{P}(A)$ is the probability of outcome $A$ and $\mathrm{P}(B)$ is the probability of outcome $B$ :

$$
\mathrm{P}(A \text { or } B)=\mathrm{P}(A)+\mathrm{P}(B)-\mathrm{P}(A \text { and } B)
$$

1 Change 25 metres to cm .

## $25 \times 100$

2500
centimetres

2 Write down two factors of 10

$$
1,2,5,10
$$

any 2 or the above


3 Work out $3.5^{2}$
12.25
$4 \quad$ Shade $\frac{2}{5}$ of this shape.


5 Write a number in the box to make the calculation correct.

$$
93.4 \div 10000=0.00934
$$

6 Write one pair of brackets in this calculation so that the answer is correct.

$$
3 \times 5-\left(2^{2}-3\right)=14
$$

7 Here are six triangles shown on a centimetre grid.


Two of these triangles are congruent.
Write down the letters of these two triangles.

and
$E$
$8 \quad$ In a shop each jar of coffee cost $£ 3.70$
Harold has $£ 50$ to spend on coffee.
Work out the greatest number of jars of coffee Harold can buy.

$$
50 \div 3.7=13.51
$$

$\qquad$
(Total for Question 8 is 2 marks)

9 Norah gets on a train at 749 am .
The train journey takes 2 hours and 45 minutes.
Norah then walks for 18 minutes to get to a meeting.
Does Norah get to the meeting before 11 am ?
You must show how you get your answer.
749
+11 ming
800
+2 hes
1000
$+34 \mathrm{mins}$
1034
+18 min
1052
(2 hrs 34 lett)
Yes

10 Here is a sequence of patterns made from sticks.

Pattern 2

Pattern 3
(a) In the space below, draw Pattern number 4

(b) Complete the table.

| Pattern number | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Number of sticks | 4 | 7 | 10 | 13 | 16 |

(c) Work out the number of sticks in pattern 10 .

$$
+3 \text { each time }
$$



11 Bradley asked a group of people to name their favourite colour. He draws a pie chart to show his results.


17 of the people said that green was their favourite colour.
Work out how many people said that blue was their favourite colour.

$$
\begin{aligned}
\frac{85}{17} & =5 \quad\left(\text { each } 1^{\circ}=5 \text { people }\right) \\
130 \div 5 & =26
\end{aligned}
$$

12
1 dollar $=0.92$ euros
(a) Change 350 dollars into euros.

$$
350 \times 0.92
$$

322
euros
(b) Change 200 euros into dollars.

$$
200 \div 0.92
$$

13 The drawing shows the positions of three towns $A, B$ and $C$ on a map.


The map has a scale of $1 \mathrm{~cm}=2.5 \mathrm{~km}$
Work out the real distance between town $A$ and town $C$.
Give your answer in kilometres.

$$
\begin{gathered}
8 \times 2.5=20 \\
15 \times 2.5=37.5 \\
20+37.5
\end{gathered}
$$

14 Cameron has some coins with a total value of 95 pence.
She has only 2 pence coins and 5 pence coins.
The ratio

$$
\text { number of } 2 \text { pence coins : number of } 5 \text { pence coins }=2: 3
$$

Work out how many 5 pence coins Cameron has.

$$
\times 2 \times 5
$$

ratio of values


$$
\begin{aligned}
& 20 p \text { in } 2 p s \\
& 75 p \text { in } 5 p s \quad 75 \div 5 \quad 15
\end{aligned}
$$

15 The scale drawing shows the positions of two towns $A$ and $B$.

Find the bearing of $A$ from $B$.


$$
360-75
$$

$$
285
$$

1660 students study a language at a school.
Each student either studies French or German.
36 of the students are boys.
$\frac{2}{3}$ of the boys study French

$$
\begin{aligned}
& \frac{2}{3} \times 36=24 \\
& 40-24=16
\end{aligned}
$$

40 students study French
Use this information to complete the frequency tree.


17
(a) Factorise
$3 a^{2}+4 a b$

$$
a(3 a+4 b)
$$

(1)
(b) Solve $3(g+9)=21$

$$
\begin{aligned}
3 g+27 & =21 \\
3 g & =-6 \\
g & =-2
\end{aligned}
$$

$$
g=-2
$$

(Total for Question 17 is $\mathbf{3}$ marks)

18 Debbie buys 4 packs of oats.
Each pack contains 750 grams of oats.
The total cost of the 4 packs is $£ 9.20$
Work out the cost per 100 g of oats.
Give your answer correct to the nearest penny.

$$
\begin{aligned}
& 3000 \mathrm{~g} \text { for } t 9.20 \\
& \div 30 \quad \div 30 \\
& 100 \mathrm{~g} \text { for } t 0.31
\end{aligned}
$$

19 The diagram shows a solid prism.


The volume of the prism is $804 \mathrm{~cm}^{3}$
Work out the value of $x$

$$
\begin{aligned}
\text { Area of cross section } & =10 \times 6+9 \times x \\
& =60+9 x
\end{aligned}
$$

$$
\text { Volume }=\text { Area of coss section } x \text { depth }
$$

$$
804=\text { Area of cross-section } \times 8
$$

$$
100.5=\text { Area or coss section }
$$

$$
\begin{aligned}
60+9 x & =100.5 \\
9 x & =40.5 \\
x & =4.5
\end{aligned}
$$

20 The frequency table shows the time taken for 100 people to travel to an event.

| Time (minutes) | Frequency |
| :---: | :---: |
| $0<\mathrm{t} \leqslant 10$ | 14 |
| $10<\mathrm{t} \leqslant 20$ | 16 |
| $20<\mathrm{t} \leqslant 30$ | 23 |
| $30<\mathrm{t} \leqslant 40$ | 29 |
| $40<\mathrm{t} \leqslant 50$ | 12 |
| $50<\mathrm{t} \leqslant 60$ | 6 |

Draw a frequency polygon to show this information.


21 Bradley gets the bus on Saturday and Sunday.
The probability that Bradley's bus will be late on any day is 0.15
Bradley draws this probability tree diagram.
The diagram is not correct.


Write down two things that are wrong with the probability tree diagram.

1 The probability of the bus not being late on Saturday should be 0.85

2 The probabilities for Sunday (after late on Saturday)
are the wrong way around. (see diagram)

22 Matt wants to invest $£ 8000$ for three years. He can choose between Bank A and Bank B.

Bank A
$1.2 \%$ compound interest per annum

Bank B
$2 \%$ compound interest in the first year $1 \%$ compound interest for each extra year

Which bank will give Matt the most interest after three years.
You must show your working.

$$
\begin{array}{c|c}
B \text { ark } A & B \text { ark } B \\
8000 \times 1.012^{3} & 8000 \times 1.02 \times 1.01^{2} \\
=\hbar 8291.47 & =\hbar 8324.02
\end{array}
$$

$$
\text { Bank } B
$$

23 The average daytime temperature for 10 days is recorded.
A shop also records its ice cream sales for each of the 10 days.
The scatter graph shows this information.

(a) What type of correlation does the scatter graph show?

(1)
(b) On the $11^{\text {th }}$ day the temperature was $12^{\circ} \mathrm{C}$.

Estimate the ice cream sales on the 11th day.
$\pm \quad 130$
(2)
(c) The shop's manager wants to use the scatter graph to predict the ice cream sales for a day with an average temperature of $2^{\circ} \mathrm{C}$. Comment on the reliability of this prediction.

$$
\text { It would not be reliable. } 2^{\circ} \mathrm{C} \text { is not }
$$

in the range of data.

24 Find $5 \%$ of $3.8 \times 10^{105}$
Give your answer in standard form

$$
\begin{aligned}
5 \% & =0.05 \times 3.8 \\
& =0.19
\end{aligned}
$$

$$
\begin{aligned}
& 0.19 \times 10^{105} \\
& 1.9 \times 10^{104}
\end{aligned}
$$

$$
1.9 \times 10^{104}
$$

(Total for Question 24 is $\mathbf{3}$ marks)

25 Verity buys 12 bottles of apple juice for a total cost of $£ 15$
Verity sells all 12 bottles at $£ 1.75$ each bottle.
Work out Verity's percentage profit.

$$
\begin{aligned}
12 \times 1.75 & =21 \\
\text { profit } & =21-15 \\
& =6 \\
\% \text { profit } & =\frac{6}{15} \times 100 \\
& =40 \%
\end{aligned}
$$

26

$$
y^{2} \times y^{a}=y^{7}
$$

$$
2+a=7
$$

(a) Find the value of $a$.

$$
\begin{equation*}
\left(y^{4}\right)^{b}=y^{12} \tag{1}
\end{equation*}
$$

(b) Find the value of $b$.

$$
4 \times b=12
$$

27 Change a speed of 81 kilometres per hour to a speed in metres per second

$$
\begin{array}{r}
81 \mathrm{~km} \text { per hour } \\
81000 \mathrm{mer} \text { hour } \\
\div 60
\end{array}
$$

1350 m per minute

$$
\div 60
$$

22.5 m per second

28 The diagram shows a pentagon.


Work out the value of $x$

$$
\begin{aligned}
& \text { Angles in a pentagon }=3 \times 180 \\
&=540^{\circ} \\
& 540-90-98-92-121
\end{aligned}
$$

29 The density of orange cordial is 1.21 grams per $\mathrm{cm}^{3}$.
The density of carbonated water is 1.01 grams per $\mathrm{cm}^{3}$.
An drink with a volume of $280 \mathrm{~cm}^{3}$ is made by mixing 1 part of orange cordial with 7 parts of carbonated water.

Work out the density of the drink.

$$
\begin{aligned}
& \text { density }=\frac{\text { total mass }}{\text { total volume }} \\
& 1: 7 \\
& 280 \div 8=35 \quad 35 \mathrm{~cm}_{3}^{3} \text { orange }
\end{aligned}
$$

$$
\begin{aligned}
& 35 \times 7=2 \\
& =d \times v
\end{aligned}
$$

$$
\text { mass }=d \times v
$$

$$
\begin{aligned}
\text { Orange: mass } & =1.21 \times 35 \\
& =42.359
\end{aligned}
$$

$$
=42.35 \mathrm{~g}
$$

$$
\begin{aligned}
\text { Water: mass } & =1.01 \times 245 \\
& =247.459
\end{aligned}
$$

$$
\begin{align*}
\text { Density } & =\frac{42.35+247.45}{280} \\
& =1.035 \tag{3}
\end{align*}
$$

(Total for Question 29 is 4 marks)


Work out the perimeter of the semicircle.
Give your answer correct to 3 significant figures.

$$
\begin{aligned}
\sin \theta & =\frac{O}{H} \\
\sin 51 & =\frac{9}{d} \\
d \sin 51 & =9 \\
\alpha & =\frac{9}{\sin 51} \\
& =11.58 \mathrm{~cm}
\end{aligned}
$$

$$
\begin{aligned}
\text { Circumference } & =\pi(11.58) \\
& =36.38 \\
\text { Half circumference } & =\frac{36.38}{2} \\
& =18.19 \\
\text { Perimeter } & =18.19+11.58 \\
& =29.8 \mathrm{~cm}
\end{aligned}
$$

31 Solve $x^{2}+3 x-54=0$

$$
\begin{aligned}
& (x+9)(x-6)=0 \\
& x=-9 \quad x=6
\end{aligned}
$$

$$
x=-9, x=6
$$

(Total for Question 31 is 3 marks)
TOTAL FOR PAPER IS 80 MARKS

