Edexcel GCSE
Mathematics (Linear) – 1MA0
SPHERES AND CONES

Materials required for examination
Ruler graduated in centimetres and millimetres, protractor, compasses, pen, HB pencil, eraser.
Tracing paper may be used.

Items included with question papers
Nil

Instructions
Use black ink or ball-point pen.
Fill in the boxes at the top of this page with your name, centre number and candidate number.
Answer all questions.
Answer the questions in the spaces provided – there may be more space than you need.
Calculators may be used.

Information
The marks for each question are shown in brackets – use this as a guide as to how much time to spend on each question.
Questions labelled with an asterisk (*) are ones where the quality of your written communication will be assessed – you should take particular care on these questions with your spelling, punctuation and grammar, as well as the clarity of expression.

Advice
Read each question carefully before you start to answer it.
Keep an eye on the time.
Try to answer every question.
Check your answers if you have time at the end.
1.

The diagram represents a cone.
The height of the cone is 12 cm.
The diameter of the base of the cone is 10 cm.

Calculate the curved surface area of the cone.
Give your answer as a multiple of \( \pi \).

\[
\text{curved surface area} = \pi rl
\]

\[
l = \sqrt{12^2 + 5^2} = 13
\]

\[
r = 5
\]

\[
\text{curved surface area} = \pi (5)(13)
\]

\[
= 65\pi
\]

\[
65\pi \text{ cm}^2
\]

(Total 3 marks)
The radius of the base of a cone is 5.7 cm. Its slant height is 12.6 cm.

Calculate the volume of the cone.
Give your answer correct to 3 significant figures.

\[
\text{Volume of cone} = \frac{1}{3} \pi r^2 h
\]

\[
r = 5.7 \\
h = \sqrt{12.6^2 - 5.7^2} \\
= 11.23699248
\]

\[
\text{Volume of cone} = \frac{1}{3} \pi (5.7)^2 (11.23699248) \\
= 382.3212348 \\
= 382 \text{ cm}^3 \quad (3 \text{sf})
\]

\[382 \text{ cm}^3\]
(Total 4 marks)
A cone has a base radius of 5 cm and a vertical height of 8 cm.

Calculate the volume of the cone.

Give your answer correct to 3 significant figures.

\[
\text{Volume} = \frac{1}{3} \pi r^2 h
\]

\[
= \frac{1}{3} (\pi) (5)^2 (8)
\]

\[
= 209.4395102 \text{ cm}^3
\]

\[
\approx 209 \text{ cm}^3 \ (3 \text{ sf})
\]

\[209 \text{ cm}^3 \ (2)\]
4. The diagram shows a child’s toy.

Diagram NOT accurately drawn

The toy is made from a cone on top of a hemisphere.
The cone and hemisphere each have radius 7 cm.
The total height of the toy is 22 cm.
Work out the volume of the toy.
Give your answer correct to 3 significant figures.

\[
\text{volume of cone} = \frac{1}{3} \pi r^2 h
\]

\[
\text{volume of hemisphere} = \frac{1}{2} \left( \frac{4}{3} \pi r^3 \right)
\]

\[
\text{total volume} = \frac{1}{3} \pi (7)^2 (15) + \frac{4}{6} \pi (7)^3
\]

\[
= 14,880.06772
\]

\[
= 14,903.384
\]

\[
14.90 \text{ cm}^3
\]

(Total 3 marks)
The diagram shows a solid hemisphere of radius 8 cm.

Work out the total surface area of the hemisphere. Give your answer correct to 3 significant figures.

\[
\text{Surface area of hemisphere} = \pi r^2 + 2\pi r^2
\]

\[
= 3\pi r^2
\]

\[
= 3\pi (8)^2
\]

\[
= 603.1857845 \text{ cm}^2
\]

\[
\approx 603 \text{ cm}^2 \text{ (3 s.f.)}
\]
A rectangular container is 12 cm long, 11 cm wide and 10 cm high. The container is filled with water to a depth of 8 cm.

A metal sphere of radius 3.5 cm is placed in the water. It sinks to the bottom.

Calculate the rise in the water level. Give your answer correct to 3 significant figures.

\[
\text{Initial volume} = 12 \times 11 \times 8 = 1056 \text{ cm}^3
\]

\[
\text{Volume of sphere} = \frac{4}{3} \pi r^3
\]

\[
= \frac{4}{3} \pi (3.5)^3
\]

\[
= 179.59438
\]

\[
\text{New volume} = 1056 + 179.59438 = 1235.59438 \text{ cm}^3
\]

\[
12 \times 11 \times h = 1235.59438
\]

\[
h = 9.360563485 \text{ cm}
\]

\[
\text{Rise} = 9.360563485 - 8 = 1.360563485 = 1.36 \text{ cm (3sf)}
\]

(Total 4 marks)
A frustum is made by removing a small cone from a similar large cone.
The height of the small cone is 20 cm.
The height of the large cone is 40 cm.
The diameter of the base of the large cone is 30 cm.
Work out the volume of the frustum.
Give your answer correct to 3 significant figures.

Big cone volume = \( \frac{1}{3} \pi (15)^2 (40) \)

Small cone volume = \( \frac{1}{3} \pi \left( \frac{7.5}{2} \right)^2 (20) \)

Frustum volume = \( \frac{1}{3} \pi (15)^2 (40) - \frac{1}{3} \pi (7.5)^2 (20) \)

\[ \approx 8246.6807 \text{ cm}^3 \]

\[ \approx 8250 \text{ cm}^3 \]

(Total 4 marks)