Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- **Answer all** questions.
- **Answer the questions in the spaces provided**
  - there may be more space than you need.
- **Calculators may be used.**
- If your calculator does not have a $\pi$ button, take the value of $\pi$ to be 3.142 unless the question instructs otherwise.
- **Diagrams are NOT** accurately drawn, unless otherwise indicated.
- You must **show all your working out**.

Information

- The total mark for this paper is 80
- The marks for **each** question are shown in brackets
  - use this as a guide as to how much time to spend on each question.

Advice

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end.
Answer ALL questions.

Write your answers in the spaces provided.

You must write down all the stages in your working.

1 Write 2148 correct to the nearest 100

\[2100\]

(Total for Question 1 is 1 mark)

2 (a) Simplify \(8x - 3x + 2x\)

\[7x\]

(1)

(b) Simplify \(4y \times 2y\)

\[8y^2\]

(1)

(Total for Question 2 is 2 marks)

3 There are 6760 people at a rugby match.
3879 of the people are men.
1241 of the people are women.
1\(\frac{1}{4}\) of the children are girls.

Work out how many boys are at the rugby match.

\[6760 - 5120 = 1640\text{ children}\]

410 Girls 1230 Boys

(Total for Question 3 is 3 marks)
4. Here is a grid showing the points A, B and C.

(a) Write down the coordinates of the point A.

(b) On the grid, mark with a cross (×) the point (1, 2).
   Label this point D.

(c) On the grid, mark with a cross (×) a point E, so that the quadrilateral ABCE is a kite.

(Total for Question 4 is 3 marks)

5. Faiza buys
   one magazine costing £2.30
   one paper costing 92p
   two identical bars of chocolate

Faiza pays with a £5 note. She gets 40p change.

Work out the cost of one bar of chocolate.

£5.00 - £0.40 = £4.60

£4.60 - £3.22 = £1.38

£1.38 ÷ 2 = 69p

(Total for Question 5 is 3 marks)
The bar chart gives information about the numbers of students in the four Year 11 classes at Trowton School.

(a) What fraction of the students in class 11A are girls?

Shola says,

"There are more boys than girls in Year 11 in Trowton School."

(b) Is Shola correct?

You must give a reason for your answer.

Boys: \[14 + 12 + 8 + 4 = 38\]
Girls: \[15 + 11 + 7 + 5 = 38\]

Shola is not correct. There are 38 boys and 38 girls.
The pie chart gives information about the 76 students in the same four Year 11 classes at Trowton School.

Number of students in Year 11 of Trowton School

Tolu says,

"It is more difficult to find out the numbers of students in each class from the pie chart than from the bar chart."

(c) Is Tolu correct?
You must give a reason for your answer.

Tolu is correct. You would have to convert the measure of each angle and then calculate angle to no. of students.

(Total for Question 6 is 5 marks)
7 Here is a number machine.

\[
\begin{array}{c}
\text{input} \rightarrow \times 3 \rightarrow -4 \rightarrow \text{output}
\end{array}
\]

(a) Work out the \textbf{output} when the input is 4

\[
4 \times 3 - 4 = 8
\]

(b) Work out the \textbf{input} when the output is 11

\[
\frac{11 + 4}{3} = 5
\]

(c) Show that there is a value of the input for which the input and the output have the same value.

\[
3x - 4 = x \Rightarrow 3x = x + 4 \Rightarrow 2x = 4 \Rightarrow x = 2
\]

\[
\text{or} \quad 2 \times 3 - 4 = 2
\]

(Total for Question 7 is 5 marks)
8 1 yard is 36 inches.
   10 cm is an approximation for 4 inches.

   Work out an approximation for the number of cm in 2 yards.

   \[
   \begin{align*}
   10 \text{ cm} &= 4 \text{ inches} \\
   1 \text{ yard} &= 36 \text{ inches} \\
   2 \text{ yards} &= 72 \text{ inches} \\
   10 \times 18 &= 180 \text{ cm} \\
   180 \text{ cm} &= 72 \text{ inches} \\
   
   72 \div 4 &= 18 \\
   \\
   180 \text{ cm} \\
   
   \end{align*}
   \]

(Total for Question 8 is 3 marks)

9 Work out 234% of 150

   \[
   2.34 \times 150 = 351
   \]

   \[
   351
   \]

(Total for Question 9 is 2 marks)
10 Here are four numbers.

\[
\begin{array}{cccc}
0.43 & \frac{3}{7} & 43.8\% & \frac{7}{16} \\
0.429 & 0.938 & 0.4375 \\
\end{array}
\]

Write these numbers in order of size.
Start with the smallest number.

\[
\frac{3}{7}, 0.43, \frac{7}{16}, 0.4375.
\]

(Total for Question 10 is 2 marks)

11 Here is a list of five numbers.

14 15 16 17 18

From the list,

(i) write down the prime number,

(ii) write down the square number.

\[
\begin{array}{c}
17 \\
16 \\
\end{array}
\]

(Total for Question 11 is 2 marks)
12. Here is a star shape.

The star shape is made from a regular hexagon and six congruent equilateral triangles. The area of the star shape is 96 cm².

Work out the area of the regular hexagon.

\[ \frac{76}{2} = 48 \]

\[ \frac{48}{cm^2} \]

(Total for Question 12 is 2 marks)
WXYZ is a quadrilateral.
XYV is a straight line.

(a) (i) Find the size of the angle marked \(a\).

\[
180 - 147 = 33^\circ
\]

(ii) Give a reason for your answer.

\textit{Angles on a straight line sum to } 180^\circ

Angle ZWX = angle WXY

(b) Work out the size of angle ZWX.

\[
\frac{360 - 145 - 33}{2} = 91^\circ
\]

(Total for Question 13 is 4 marks)
14 The total weight of 3 tins of beans and 4 jars of jam is 2080 g. 
The total weight of 5 tins of beans is 2000 g.

Work out the weight of 1 tin of beans and the weight of 1 jar of jam.

\[ \begin{align*}
\frac{1}{5} \left( \frac{5 \text{ beans} = 2000 \text{ g}}{1 \text{ beans} = 400 \text{ g}} \right) &= \frac{1}{5} \times 400 \text{ g} \\
3 \text{ beans} + 4 \text{ jam} &= 2080 \\
1200 + 4 \text{ jam} &= 2080 \\
4 \text{ jam} &= 880 \\
\text{1 jam} &= 220 \text{ g} \\
\text{tin of beans} &= 400 \text{ g} \\
\text{jar of jam} &= 220 \text{ g} \\
\end{align*} \]

(Total for Question 14 is 4 marks)
There are 25 boys and 32 girls in a club.

$\frac{2}{5}$ of the boys and $\frac{1}{2}$ of the girls walk to the club.

The club leader picks at random a child from the children who walk to the club.

Work out the probability that this child is a boy.

\[
\frac{2}{5} \times 25 = 10 \text{ boys} \\
\frac{1}{2} \times 32 = 16 \text{ girls}
\]

\[
\frac{10}{26}
\]

(Total for Question 15 is 3 marks)
16 Change 72 km/h into m/s.

\[ \begin{align*}
&72 \text{ km/h} \\
&\times 1000 \\
&72000 \text{ m/h} \\
&\div 60 \\
&1200 \text{ m/min} \\
&\div 60 \\
&20 \text{ m/s} \\
\end{align*} \]

\[ \quad 20 \text{ m/s} \]

(Total for Question 16 is 3 marks)
17 Here is a rectangle made of card.

The measurements in the diagram are in centimetres.
Lily fits four of these rectangles together to make a frame.

\[ y \quad 2x \]

The perimeter of the inside of the frame is \( P \) cm.
(a) Show that \( P = 8x - 4y \)

\[
P = 2x + 2x + 2x - y - y + 2x - y - y
\]

\[
= 8x - 4y
\]

Magda says,

"When \( x \) and \( y \) are whole numbers, \( P \) is always a multiple of 4."

(b) Is Magda correct?
You must give a reason for your answer.

Magda is correct. Multiples of 8 and 4 are multiples of 4. If you subtract a multiple of 4 from another multiple of 4 you get a multiple of 4.

\begin{align*}
0 \to & \quad 4(2x - y) \\
4 \text{ times table}
\end{align*}

(Total for Question 17 is 4 marks)
The diagram shows a trapezium $ABCD$ and two identical semicircles.

The centre of each semicircle is on $DC$.

Work out the area of the shaded region.
Give your answer correct to 3 significant figures.

Area of trapezium $= \frac{12 + 28}{2} \times 14$

$= 280 \text{ cm}^2$

Area of circle $= \pi \times 3^2$

$= 9\pi \approx 28.27433388$

$280 - 9\pi = 252 \text{ (3sf)}$

$252 \text{ cm}^2$

(Total for Question 18 is 4 marks)
19 Asif is going on holiday to Turkey.

The exchange rate is £1 = 3.5601 lira.

Asif changes £550 to lira.

(a) Work out how many lira he should get.
   Give your answer to the nearest lira.

\[ 550 \times 3.5601 = 1958 \text{ (nearest lira)} \]

Asif sees a pair of shoes in Turkey.
The shoes cost 210 lira.

Asif does not have a calculator.
He uses £2 = 7 lira to work out the approximate cost of the shoes in pounds.

(b) Use £2 = 7 lira to show that the approximate cost of the shoes is £60

\[ \frac{\£2}{7} \times 3 = \£6 \times 3 = \£18 \]

\[ \frac{\£2}{7} \times 10 = \£20 \]

\[ (\frac{\£2}{7} \times 10) \times 3 = 1958 \text{ lira} \]

(c) Is using £2 = 7 lira instead of using £1 = 3.5601 lira a sensible start to Asif's method to work out the cost of the shoes in pounds?

You must give a reason for your answer.

Yes, £1 = 3.5 lira is close to the actual exchange rate and he doesn't have a calculator.

(Total for Question 19 is 5 marks)
20 Here are the first six terms of a Fibonacci sequence.

\[1 \quad 1 \quad 2 \quad 3 \quad 5 \quad 8 \quad 13 \quad 21 \quad 34\]

The rule to continue a Fibonacci sequence is,

the next term in the sequence is the sum of the two previous terms.

(a) Find the 9th term of this sequence.

\[\text{The first three terms of a different Fibonacci sequence are}\]
\[a \quad b \quad a+b \quad a+2b \quad 2a+3b \quad 3a+5b\]

(b) Show that the 6th term of this sequence is \(3a+5b\)

\[b + a+b = a+2b\]
\[a+b + a+2b = 2a+3b\]
\[a+2b + 2a+3b = 3a+5b\]

(c) Given that the 3rd term is 7 and the 6th term is 29,

\[a+b = 7 \quad \text{(1)}\]
\[3a+5b = 29 \quad \text{(2)}\]
\[3a+3b = 21 \quad \text{(1) x 3}\]
\[2b = 8\]
\[b = 4\]
\[a = 3 \quad \text{(3)}\]
\[a + 4 = 7\]
\[a = 3\]

(Total for Question 20 is 6 marks)
21 In a survey, the outside temperature and the number of units of electricity used for heating were recorded for ten homes.

The scatter diagram shows this information.

\[
\begin{array}{c|c}
\text{Number of units used} & \text{Outside temperature °C} \\
\hline
80 & 0 \\
70 & 5 \\
60 & 10 \\
50 & 15 \\
40 & 20 \\
30 & 25 \\
20 & 30 \\
\end{array}
\]

Molly says,

"On average the number of units of electricity used for heating decreases by 4 units for each °C increase in outside temperature."

(a) Is Molly right?
Show how you get your answer.

\[
\frac{38}{15} = 2.53 \quad \text{Molly is incorrect.}
\]

\text{decrease is less than 4 units per °C.}

(3)

(b) You should not use a line of best fit to predict the number of units of electricity used for heating when the outside temperature is 30°C.

Give one reason why.

\[
\text{It is outside of the range in the survey.}
\]

(1)

(Total for Question 21 is 4 marks)
22 Henry is thinking of having a water meter.

These are the two ways he can pay for the water he uses.

Water Meter
A charge of £28.20 per year
plus
91.22p for every cubic metre of water used
1 cubic metre = 1000 litres

No Water Meter
A charge of £107 per year

Henry uses an average of 180 litres of water each day.

Use this information to determine whether or not Henry should have a water meter.

\[
\begin{align*}
180 \text{ litres per day} \\
180 \times 365 &= 65700 \text{ litres per year} \\
\frac{65700}{1000} &= 65.7 \text{ cubic metres} \\
65.7 \times 91.22 &= 5993.154 \text{ p} \\
&= \text{£59.93} \\
128.20 - \text{£88.13} &= \text{£40.07}
\end{align*}
\]

Henry should have a water meter.

\[
\text{£88.13 < £107}
\]

(Total for Question 22 is 5 marks)
A and B are two companies.

The table shows some information about the sales of each company and the number of workers for each company in 2004 and in 2014.

<table>
<thead>
<tr>
<th></th>
<th>Company A</th>
<th></th>
<th>Company B</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Sales (£ millions)</td>
<td>Number of workers</td>
<td>Sales (£ millions)</td>
</tr>
<tr>
<td>2004</td>
<td>320</td>
<td>2960</td>
<td>48</td>
</tr>
<tr>
<td>2014</td>
<td>388</td>
<td>3200</td>
<td>57</td>
</tr>
</tbody>
</table>

(a) Work out the percentage increase in sales from 2004 to 2014 for Company A.

\[
\% \text{ change} = \frac{\text{change}}{\text{original}} \times 100
\]

\[
\frac{388 - 320}{320} \times 100 = 21.25\% \quad (2)
\]

(b) Which company had the most sales per worker in 2014, Company A or Company B?
You must show how you get your answer.

\[
A: \quad \frac{388}{3200} = 0.12125 \\
B: \quad \frac{57}{640} = 0.0890625
\]

Company A had the most sales per worker.

(Total for Question 23 is 5 marks)

TOTAL FOR PAPER IS 80 MARKS