Edexcel GCSE
Mathematics (Linear) – 1380
Paper 3 (Non-Calculator)

Higher Tier
Monday 7 June 2010 – Afternoon
Time: 1 hour 45 minutes

Materials required for examination
Ruler graduated in centimetres and millimetres, protractor, compasses, pen, HB pencil, eraser.
Tracing paper may be used.

Items included with question papers
Nil

Instructions to Candidates
In the boxes above, write your centre number, candidate number, your surname, initials and signature.
Check that you have the correct question paper.
Answer ALL the questions. Write your answers in the spaces provided in this question paper.
You must NOT write on the formulae page.
Anything you write on the formulae page will gain NO credit.
If you need more space to complete your answer to any question, use additional answer sheets.

Information for Candidates
The marks for individual questions and the parts of questions are shown in round brackets: e.g. (2).
There are 27 questions in this question paper. The total mark for this paper is 100.
There are 24 pages in this question paper. Any blank pages are indicated.
Calculators must not be used.

Advice to Candidates
Show all stages in any calculations.
Work steadily through the paper. Do not spend too long on one question.
If you cannot answer a question, leave it and attempt the next one.
Return at the end to those you have left out.
Volume of a prism = area of cross section × length

Volume of sphere = \( \frac{4}{3} \pi r^3 \)
Surface area of sphere = \( 4\pi r^2 \)

Volume of cone = \( \frac{1}{3} \pi r^2 h \)
Curved surface area of cone = \( \pi rl \)

In any triangle ABC

The Sine Rule
\[
\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}
\]

The Cosine Rule
\[ a^2 = b^2 + c^2 - 2bc \cos A \]

Area of triangle = \( \frac{1}{2} ab \sin C \)

The Quadratic Equation
The solutions of \( ax^2 + bx + c = 0 \)
where \( a \neq 0 \), are given by
\[ x = \frac{-b \pm \sqrt{(b^2 - 4ac)}}{2a} \]
1. Simplify $6x + 9y + 2x - 3y$

\[..............................\]

**Q1**

(Total 2 marks)

2. Here are the weights, in grams, of 16 eggs.

<table>
<thead>
<tr>
<th>47</th>
<th>45</th>
<th>50</th>
<th>53</th>
<th>43</th>
<th>61</th>
<th>53</th>
<th>62</th>
</tr>
</thead>
<tbody>
<tr>
<td>58</td>
<td>56</td>
<td>57</td>
<td>47</td>
<td>55</td>
<td>62</td>
<td>58</td>
<td>58</td>
</tr>
</tbody>
</table>

Draw an ordered stem and leaf diagram to show this information. You must include a key.

Key:

**Q2**

(Total 3 marks)
3. \[ PQR \text{ is a straight line.} \]
\[ PT = PQ. \]

(i) Work out the value of \( y \).

(ii) Give reasons for your answer.

.................................................................
.................................................................
.................................................................

(Total 4 marks)
4. Nigel travelled from his home to his friend’s house 40 km away. He stayed at his friend’s house for 30 minutes. Nigel then travelled home.

Here is part of the distance-time graph for Nigel’s journey.

(a) At what time did Nigel leave home?

(b) How far was Nigel from home at 10 20?

(c) Complete the distance-time graph.

(Nigel arrived home at 11 50)

(Total 3 marks)
Triangle T has been drawn on the grid.

Rotate triangle T 180° about the point (1, 0).
Label the new triangle A.

(Q5) (Total 2 marks)
6. Describe fully the single transformation which maps shape \( P \) onto shape \( Q \).

.............................................................................................................................

.............................................................................................................................

(Total 3 marks)

7. Anna and Bill share £40 in the ratio 2 : 3

Work out how much each person gets.

Anna £..............................

Bill £..............................

(Total 3 marks)
8. Sasha carried out a survey of 60 students. She asked them how many CDs they each have.

This table shows information about the numbers of CDs these students have.

<table>
<thead>
<tr>
<th>Number of CDs</th>
<th>0 – 4</th>
<th>5 – 9</th>
<th>10 – 14</th>
<th>15 – 19</th>
<th>20 – 24</th>
</tr>
</thead>
<tbody>
<tr>
<td>Frequency</td>
<td>8</td>
<td>11</td>
<td>9</td>
<td>14</td>
<td>18</td>
</tr>
</tbody>
</table>

(a) Write down the class interval containing the median.

..................................

(b) On the grid, draw a frequency polygon to show the information given in the table.
9. 

Diagram NOT accurately drawn

Work out the volume of the triangular prism.

................. cm$^3$

Q9
(Total 2 marks)

10. Work out $4.52 \times 36$

.................

Q10
(Total 3 marks)
11. There are 300 people in the cinema.

\[ \frac{1}{6} \text{ of the 300 people are boys.} \]

\[ \frac{3}{10} \text{ of the 300 people are girls.} \]

The rest of the people are adults.

Work out how many people are adults.

\[ \frac{1}{6} \times 300 = 50 \] boys

\[ \frac{3}{10} \times 300 = 90 \] girls

Adults: 300 - (50 + 90) = 160

12. Diagram NOT accurately drawn

Work out the size of an exterior angle of a regular pentagon.

\[ \frac{360}{5} = 72 \] degrees
13. Anil wants to find out how many DVDs people buy.

He uses this question on a questionnaire.

How many DVDs do you buy?

1 – 5  5 – 10  10 – 15  15 – 20

Write down two different things wrong with this question.

1 .......................................................................................................................... ................
............................................................................................................................. .................

2 .......................................................................................................................... ................
............................................................................................................................. .................

(Total 2 marks)
14. (a) Complete the table of values for \( y = x^2 + x - 3 \)

<table>
<thead>
<tr>
<th>( x )</th>
<th>-4</th>
<th>-3</th>
<th>-2</th>
<th>-1</th>
<th>0</th>
<th>1</th>
<th>2</th>
</tr>
</thead>
<tbody>
<tr>
<td>( y )</td>
<td>9</td>
<td>-1</td>
<td>-3</td>
<td>3</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

(2)

(b) On the grid below, draw the graph of \( y = x^2 + x - 3 \) for values of \( x \) from -4 to 2

(2)
(c) Use your graph to find estimates for the solutions of \( x^2 + x - 3 = 0 \)

\[ x = \ldots \ldots \ldots \ldots \ldots \ldots \]

\[ x = \ldots \ldots \ldots \ldots \ldots \ldots \]

(1)

15. Express 180 as a product of its prime factors.

\[ \ldots \ldots \ldots \ldots \ldots \ldots \]

(Q15) (Total 3 marks)

16. Work out \( \frac{3\frac{1}{4}}{4} \times 2\frac{2}{3} \)

Give your answer in its simplest form.

\[ \ldots \ldots \ldots \ldots \ldots \ldots \]

(Q16) (Total 3 marks)
17. (a) Factorise \( 3x + 12 \)

\[ \text{.....................................} \]

(b) Solve \( 4(2x - 3) = 5x + 7 \)

\[ x = \text{.....................................} \]

(c) Expand and simplify \((y + 4)(y + 5)\)

\[ \text{.....................................} \]

(d) Factorise fully \( 8x^2 + 12xy \)

\[ \text{.....................................} \]

Q17

(Total 8 marks)
18.

Diagrams NOT accurately drawn

Triangles ABC and PQR are mathematically similar.

Angle A = angle P.
Angle B = angle Q.
Angle C = angle R.
AC = 4 cm.
BC = 12 cm.
PR = 6 cm.
PQ = 15 cm.

(a) Work out the length of QR.

................................cm
(2)

(b) Work out the length of AB.

................................cm
(2) Q18
(Total 4 marks)
19. Arwen buys a car for £4000
   The value of the car depreciates by 10% each year.
   Work out the value of the car after two years.

£ ...................................

20. (a) Here are some expressions.

<p>| | | | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>$a^3b$</td>
<td>$a^2(c+b)$</td>
<td>$4abc$</td>
<td>$ab+c^3$</td>
<td>$4\pi c^2$</td>
</tr>
</tbody>
</table>

The letters $a$, $b$, and $c$ represent lengths.
$\pi$ and 4 are numbers that have no dimension.

**Two** of the expressions could represent volumes.
Tick the boxes (✓) underneath these two expressions.

The volume of this cube is 8 m$^3$.

(b) Change 8 m$^3$ into cm$^3$.

............... cm$^3$
21. Solve the simultaneous equations

\[3x + 2y = 8\]
\[2x + 5y = -2\]

\[x = \ldots\ldots\ldots\ldots\ldots\]
\[y = \ldots\ldots\ldots\ldots\ldots\]

Q21

(Total 4 marks)
22. The table gives some information about the delays, in minutes, of 80 flights.

<table>
<thead>
<tr>
<th>Delay (n minutes)</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>0 &lt; n ≤ 20</td>
<td>16</td>
</tr>
<tr>
<td>20 &lt; n ≤ 30</td>
<td>26</td>
</tr>
<tr>
<td>30 &lt; n ≤ 40</td>
<td>23</td>
</tr>
<tr>
<td>40 &lt; n ≤ 50</td>
<td>10</td>
</tr>
<tr>
<td>50 &lt; n ≤ 60</td>
<td>5</td>
</tr>
</tbody>
</table>

(a) Write down the modal class interval.

....................................

(1)

(b) Complete the cumulative frequency table.

<table>
<thead>
<tr>
<th>Delay (n minutes)</th>
<th>Cumulative Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>0 &lt; n ≤ 20</td>
<td></td>
</tr>
<tr>
<td>0 &lt; n ≤ 30</td>
<td></td>
</tr>
<tr>
<td>0 &lt; n ≤ 40</td>
<td></td>
</tr>
<tr>
<td>0 &lt; n ≤ 50</td>
<td></td>
</tr>
<tr>
<td>0 &lt; n ≤ 60</td>
<td></td>
</tr>
</tbody>
</table>

(1)

(c) On the grid opposite, draw a cumulative frequency graph for your table.

(2)

(d) Use your graph to find an estimate for

(i) the median delay,

.......................... minutes

(ii) the interquartile range of the delays.

.......................... minutes

(3)
Q22

(Total 7 marks)
23. A straight line passes through \((0, -2)\) and \((3, 10)\).

Find the equation of the straight line.

Diagram NOT accurately drawn

24. Find the value of

(i) \(6^0\)

(ii) \(64^{\frac{1}{2}}\)

(iii) \(\left(\frac{27}{8}\right)^{\frac{2}{3}}\)
25.

\[ \triangle ABC \text{ is a right-angled triangle.} \]

All the measurements are in centimetres.

\[ AB = x \]
\[ BC = (x + 2) \]
\[ AC = (x + 4) \]

(a) Show that \( x^2 - 4x - 12 = 0 \)

(b) (i) Solve \( x^2 - 4x - 12 = 0 \)

................................................................

(ii) Hence, write down the length of \( AC \).

\[ AC = \ldots \ldots \ldots \ldots \text{cm} \]

(Total 7 marks)
26. There are 3 orange sweets, 2 red sweets and 5 yellow sweets in a bag.

Sarah takes a sweet at random.
She eats the sweet.
She then takes another sweet at random.

Work out the probability that both the sweets are the same colour.
27.

$P$, $Q$ and $T$ are points on the circumference of a circle, centre $O$. The line $ATB$ is the tangent at $T$ to the circle.

$PQ = TQ$.

Angle $ATP = 58^\circ$.

Calculate the size of angle $OTQ$.

Give a reason for each stage in your working.

................................... °

(Total 5 marks)

TOTAL FOR PAPER: 100 MARKS

END